

$termvar, x, y$	term variable		
$t$	::=		term
		$x$	variable
		$\lambda x.t$	bind $x$ in $t$ lambda
		$t t'$	app
		$(t)$	S
		$[t/x]t'$	M
$v$	::=		value
		$\lambda x.t$	lambda
$terminals$	::=		
		$\lambda$	
		$\longrightarrow$	
		$\in$	
		$\neq$	
		$\equiv_\alpha$	
		$\equiv_\beta$	
		FV	
		$\notin$	
$formula$	::=		
		$judgement$	
		$x \neq x'$	M
		$x \notin FV(t)$	M
$Jop$	::=		
		$t_1 \longrightarrow t_2$	$t_1$ reduces to $t_2$
		$x \in FV(t)$	free variable
		$t \equiv_\alpha t'$	alpha equivalence
		$t \equiv_\beta t'$	beta equivalence
$judgement$	::=		
		$Jop$	
$user\_syntax$	::=		
		$termvar$	
		$t$	
		$v$	
		$terminals$	
		$formula$	

$t_1 \longrightarrow t_2$   $t_1$  reduces to  $t_2$

$$\frac{}{(\lambda x.t_{12}) v_2 \longrightarrow [v_2/x]t_{12}} \text{ AX\_APP}$$

$$\frac{t_1 \longrightarrow t'_1}{t_1 t \longrightarrow t'_1 t} \text{ CTX\_APP\_FUN}$$

$$\frac{t_1 \longrightarrow t'_1}{v t_1 \longrightarrow v t'_1} \text{ CTX\_APP\_ARG}$$

$x \in \text{FV}(t)$  free variable

$$\frac{}{x \in \text{FV}(x)} \text{VAR}$$

$$\frac{x \in \text{FV}(t_1)}{x \in \text{FV}(t_1 t_2)} \text{APP\_L}$$

$$\frac{x \in \text{FV}(t_2)}{x \in \text{FV}(t_1 t_2)} \text{APP\_R}$$

$$\frac{x \in \text{FV}(t)}{x \neq y} \text{LAM}$$

$$\frac{x \neq y}{x \in \text{FV}(\lambda y.t)} \text{LAM}$$

$t \equiv_\alpha t'$  alpha equivalence

$$\frac{}{t \equiv_\alpha t} \text{AEQ\_ID}$$

$$\frac{t \equiv_\alpha t'}{t' \equiv_\alpha t} \text{AEQ\_SYM}$$

$$\frac{t \equiv_\alpha t' \quad t' \equiv_\alpha t''}{t \equiv_\alpha t''} \text{AEQ\_TRANS}$$

$$\frac{t_1 \equiv_\alpha t'_1 \quad t_2 \equiv_\alpha t'_2}{t_1 t_2 \equiv_\alpha t'_1 t'_2} \text{AEQ\_APP}$$

$$\frac{t \equiv_\alpha t'}{\lambda x.t \equiv_\alpha \lambda x.t'} \text{AEQ\_LAM}$$

$$\frac{x' \notin \text{FV}(t)}{\lambda x.t \equiv_\alpha \lambda x'. [x'/x]t} \text{AEQ\_SUBST}$$

$t \equiv_\beta t'$  beta equivalence

$$\frac{}{t \equiv_\beta t} \text{BEQ\_ID}$$

$$\frac{t \equiv_\beta t'}{t' \equiv_\beta t} \text{BEQ\_SYM}$$

$$\frac{t \equiv_\beta t' \quad t' \equiv_\beta t''}{t \equiv_\beta t''} \text{BEQ\_TRANS}$$

$$\frac{t_1 \equiv_\beta t'_1 \quad t_2 \equiv_\beta t'_2}{t_1 t_2 \equiv_\beta t'_1 t'_2} \text{BEQ\_APP}$$

$$\frac{t \equiv_\beta t'}{\lambda x.t \equiv_\beta \lambda x.t'} \text{BEQ\_LAM}$$

$$\frac{}{(\lambda x.t) t' \equiv_\beta [t'/x]t} \text{BEQ\_SUBST}$$

Definition rules: 19 good 0 bad  
 Definition rule clauses: 38 good 0 bad